MHD HEAT AND MASS TRANSFER UNSTEADY FLOW OF A MICROPOLAR FLUID THROUGH A POROUS MEDIUM WITH INDUCED MAGNETIC FIELD

Md. Mohidul Haque and Md. Mahmud Alam

Mathematics Discipline, Khulna University, Khulna, Bangladesh

ABSTRACT

MHD free convective heat and mass transfer unsteady flow of a micropolar fluid past an infinite vertical porous plate through a porous medium has been observed under the action of a strong magnetic field taking into account the induced magnetic field with a constant heat source. It is considered that the porous plate is subjected to constant heat and mass fluxes. The mathematical model of the problem is solved numerically by the unconditionally stable implicit finite difference method. The approximate value of all the flow variables as velocity, angular velocity, induced magnetic field, fluid temperature and species concentration are computed in this work. Also the profiles of the above mentioned quantities are shown in figures and the effects of important parameters on the flow variables are discussed briefly. Finally, a comparison with previous work is tabulated here.

Keywords: MHD Heat and Mass Transfer, Micropolar Fluid, Porous Medium, Induced Magnetic Field

1. INTRODUCTION

The induced magnetic field is arisen due to a strong magnetic field. The study with induced magnetic field is of great interest in astrophysics and geophysics to investigate the stellar and solar structures, interstellar matter, radio propagation through the ionosphere etc. Since the problems with induced magnetic field play a decisive role in a number of industrial applications such as fiber or granular insulation, liquid-metals, electrolytes, ionized gases as well as the geothermal systems, Chaudhary and Sharma[1] have studied the induced magnetic field effect on a combined heat and mass transfer steady flow over a vertical plate with constant heat and mass fluxes. Numerical solutions of the same problem in case of two dimensional flows have been calculated by Alam et al.[2]. Recently, the induced magnetic field effects on mixed convective transient heat and mass transfer flow with constant heat and mass fluxes have been investigated by Haque and Alam[3].

Micropolar fluids are those, which contain dilute suspension of small, rigid, cylindrical macromolecules with individual motions that support stress and body moments, which are influenced by spin inertia. Eringen[4] was the first author to propose a theory of molecular fluids taking into account the inertial characteristics of the substructure particles, which are allowed to undergo rotation. Physically, the micropolar fluids contain suspended metal or dust particles. It has many practical applications, for example analyzing the behavior of exotic lubricants, the flow of colloidal suspensions or polymeric fluids, liquid crystals, additive suspensions, human or animal blood and turbulent shear flow. The free convective micropolar fluid flow induced by the simultaneous action of buoyancy forces is of great interest in nature and in many industrial applications as drying processes, solidification of binary alloy as well as in astrophysics, geophysics and oceanography. Jena and Mathur[5] obtained a similarity solution for laminar free convective flow of thermo-micropolar fluid from a non-isothermal vertical flat plate. A free convective mass transfer flow for a micropolar fluid bounded by a vertical surface under the action of a transverse magnetic field is observed by El-Amin[6]. Quit recently, an unsteady free convective heat and mass transfer flow of a micropolar fluid through a porous medium under the action of a transverse magnetic field with a constant heat source has been investigated by Haque et al.[7]. In the present work we want to apply a strong magnetic field that induced another magnetic field on the above problem.

Hence our aim is to investigate the thermal diffusion effect on the free convective heat and mass transfer MHD unsteady flow of a micropolar fluid past an infinite vertical porous plate through a porous medium in the present of a strong magnetic field with constant heat and mass fluxes.

2. MATHEMATICAL MODEL

A transient free convective heat and mass transfer MHD flow of electrically conducting, incompressible, viscous micropolar fluid past an electrically non-
conducting infinite vertical porous plate bounded by a porous medium with a constant heat source is considered here. The flow is assumed to be in the x-direction, which is chosen along the plate in upward direction and y-axis is normal to it. A strong uniform magnetic field is applied normal to the flow region that induced another magnetic field \( \mathbf{H} \). Initially, it is considered that the fluid particles and the plate are at rest at same temperature \( \overline{T} = T_{w} \) with same concentration level \( \overline{C} = C_{w} \) at all points, where \( T_{w} \) and \( C_{w} \) are fluid temperature and species concentration of uniform flow respectively. The physical configuration and coordinate system of the problem is presented in Fig. 1.

In addition, the magnetic Reynolds number of the flow is taken to be large enough so that the induced magnetic field is of the form \( \mathbf{H} = H_{x}, H_{y}, 0 \) is applicable. The divergence equation of Maxwell’s equation \( \nabla \mathbf{H} = 0 \) for the magnetic field gives \( H_{z} = \text{constant} = H_{0} \) (say).

It is considered that the microrotation vector is of the form \( \mathbf{G} = 0, 0, \overline{T} \) and the plate is of infinite extent with the fluid motion is unsteady, hence all the flow variables will depend only upon \( y \) and time.

Within the framework of the above stated assumptions and using the dimensionless quantities,

\[
\nu = \frac{\nu_{e}}{\nu}, \quad Y = \frac{yV_{e}}{\nu}, \quad U = \frac{u}{V_{e}}, \quad \tau = \frac{V_{e}^{2}}{\nu}, \quad \Gamma = \frac{T_{w}V_{e}}{\nu}, \quad H = \sqrt{\frac{\mu_{e} H}{\rho V_{e}}}, \quad T = \frac{\kappa V_{e}^{2}}{Q V_{e}}, \quad C = \frac{\rho_{e}}{\rho_{f}} \overline{C} - C_{w}, \quad \beta = \frac{D_{e} V_{e}^{2}}{m V_{e}}
\]

with parameters, \( G_{i} = \frac{G_{i}^{*} V_{e}^{2}}{Q V_{e}^{2}} \), \( G_{n} = \frac{G_{n}^{*} V_{e}^{2}}{D_{e} V_{e}^{2}} \), \( \Delta = \frac{\tau}{\nu}, \quad M = \frac{H_{0}^{2}}{\nu^{2}}, \quad P_{a} = \frac{\nu \sigma \mu_{0}}{\nu V_{e}^{2}}, \quad D_{z} = \frac{V_{e}^{2}}{Y_{e}^{2}} \), \( E_{i} = \frac{Q V_{e}^{2}}{2 \rho} \), \( \lambda = \frac{\nu V_{e}}{\rho j V_{e}^{2}} \), \( P_{s} = \frac{\nu \rho_{e} c_{p}}{\kappa} \), \( S_{a} = \frac{V_{e}^{2}}{D_{e}} \), \( S_{e} = \frac{Q D_{e} \kappa_{0}}{m k V_{e} c_{p}} \), \( \Lambda = \frac{\gamma}{\nu j \rho} \) as well as \( \alpha = \frac{Q V_{e}^{2}}{k V_{e}^{2}} \),

the equations relevant to the unsteady problem are governed by the following non-dimensional system of coupled non-linear partial differential equations under the boundary-layer approximations,

\[
\frac{\partial U}{\partial t} + \frac{\partial U}{\partial Y} = G_{i} T + G_{i} C + 1 + \Delta \frac{\partial U}{\partial Y} + \Delta \frac{\partial U}{\partial T} - D_{i} U + M \frac{\partial H}{\partial Y}
\]

\[
\frac{\partial H}{\partial t} + \frac{\partial H}{\partial Y} = M \frac{\partial U}{\partial Y} + \frac{\partial H}{\partial Y} + \frac{\partial H}{\partial T} - \Lambda \left( 2 \Gamma + \frac{\partial U}{\partial Y} \right)
\]

\[
\frac{\partial T}{\partial t} + \frac{\partial T}{\partial Y} = 1 \frac{\partial T}{\partial Y} + 1 + \Delta E_{i} \left( \frac{\partial U}{\partial Y} \right)^{2} + E_{s} \left( \frac{\partial H}{\partial Y} \right)^{2} - \alpha_{T} \frac{\partial C}{\partial Y} = \frac{\partial C}{\partial Y}
\]

also the appropriate initial and boundary conditions are given below when the plate is subjected to constant heat and mass fluxes,

\[
t \leq 0, \quad U = 0, \quad \Gamma = 0, \quad H = 0, \quad T = 0, \quad C = 0 \quad \text{everywhere}
\]

\[
t > 0, \quad U = 0, \quad \Gamma = -1, \quad H = 1, \quad \frac{\partial C}{\partial Y} = -1 \quad \text{at} \quad Y = 0
\]

\[
U = 0, \quad \Gamma = 0, \quad H = 0, \quad T = 0, \quad C = 0 \quad \text{as} \quad Y \rightarrow \infty
\]

3. NUMERICAL SOLUTIONS

To solve the above non-dimensional system by the unconditionally stable implicit finite difference method, it is required a set of finite difference equations. In this case, the region within the boundary layer is divided by some perpendicular lines of Y axis, where Y-axis is normal to the plate as shown in Fig. 2.

It is assumed that the maximum length of boundary layer
is $Y_{\text{max}} = 20$ as corresponds to $Y \to \infty$ i.e. $Y$ varies from 0 to 20 and the number of grid spacing in $Y$ directions is $m = 100$ , hence the constant mesh size along $Y$ axis becomes $\Delta Y = 0.20$ $0 \leq Y \leq 20$ with a smaller time-step $\Delta t = 0.01$.

Using the implicit finite difference approximations, we have the following appropriate set of finite difference equations,

$$\frac{U_i^{n+1} - U_i^n}{\Delta t} - \frac{U_{i+1}^n - U_i^n}{\Delta Y} = G_i T_i^{n+1} + G_i C_i^{n+1} + M \frac{H_i^{n+1} - H_i^n}{\Delta Y}$$

$$-D_i U_i^n + 1 + \Delta \left( \frac{U_i^{n+1} - 2U_i^n + U_{i-1}^n}{\Delta Y} + \Delta \frac{\Gamma_{i+1} - \Gamma_i}{\Delta Y} \right)$$

$$\frac{\Gamma_{i+1} - \Gamma_i}{\Delta Y} - \frac{\Gamma_{i-1} - \Gamma_{i-2}}{\Delta Y} = \lambda \left[ \frac{2\Gamma_i - U_i^{n+1}}{\Delta Y} \right]$$

$$\frac{H_i^{n+1} - H_i^n}{\Delta Y} = \frac{H_{i+1}^n - 2H_i^n + H_{i-1}^n}{\Delta Y} - \lambda \left( \frac{2H_i^n - U_i^{n+1}}{\Delta Y} \right)$$

$$\frac{T_i^{n+1} - T_i^n}{\Delta t} - \frac{T_{i+1}^n - T_{i-1}^n}{\Delta Y} = \frac{T_{i+1}^n - 2T_i^n + T_{i-1}^n}{\Delta Y} \frac{E_i \left( H_i^n - H_{i-1}^n \right)}{\Delta Y}$$

$$+ 1 + \Delta \left( \frac{U_i^{n+1} - U_i^n}{\Delta Y} \right) - \frac{\alpha P_i T_i^{n+1}}{P_i}$$

$$\frac{C_i^{n+1} - C_i^n}{\Delta t} - \frac{C_{i+1}^n - 2C_i^n + C_{i-1}^n}{\Delta Y} = \frac{S_i \left( T_i^{n+1} - 2T_i^n + T_{i-1}^n \right)}{\Delta Y}$$

with the finite difference initial and boundary conditions,

$$U_0^n = 0, \quad G_0^n = 0, \quad H_0^n = 0, \quad T_0^n = 0, \quad C_0^n = 0$$

$$U_L^n = 0, \quad G_L^n = 0, \quad H_L^n = 0, \quad T_L^n = 0, \quad C_L^n = 0 \quad \text{where} \quad L \to \infty$$

Here the subscript $i$ designates the grid points with $Y$ coordinate and the superscript $n$ represents a value of time, $t = n \Delta t$ where $n = 0, 1, 2, 3, 4, \ldots \ldots$ The velocity, angular velocity, induced magnetic field, temperature and concentration at all interior nodal points may be computed by successive applications of the above finite difference equations.

4. RESULTS AND DISCUSSION

To investigate the practical situation of the problem, we have obtained the numerical values of the dimensionless velocity, angular velocity, induced magnetic field, temperature and concentration within the boundary layer for the turbulent boundary layer flow i.e. the value of microrotational constant(s) is chosen 1.0. Because of the great importance of cooling problem in nuclear engineering in connection with the cooling of reactors, the value of the Grashof number and modified Grashof number for heat transfer is taken positive. Since the most important fluids are atmospheric air, salt water and water so the results are limited to $P_i = 0.71$ (Prandtl number for air at 20°C), $P_i = 1.0$ (Prandtl number for salt water at 20°C) and $P_i = 7.0$ (Prandtl number for water at 20°C). In this study, the values of other parameters are chosen arbitrarily.

In order to get the steady state solutions of the problem, the computations have been carried out up to $t = 10$. We observed that the values of this computation, however, show little changes after $t = 4$. Thus the solution at $t = 10$ are essentially steady-state solutions. Hence the velocity, angular velocity, induced magnetic field, temperature and concentration profiles are drawn at $t = 1.0, 2.0$ and 10.0.

The velocity, angular velocity, induced magnetic field, temperature and concentration distributions versus $Y$ are illustrated in Figs. 3-18. The effect of the magnetic force number on the velocity field is presented in Fig. 3. It is observed that $U$ decreases near the plate in case of strong $M$ but far away from the plate the increase of $M$ leads to an increase in velocity. The effect of Darcy on the velocity field is plotted in Fig. 4. From this figure we see that the velocity decreases with the increase of $D$. Fig. 5 shows that the velocity increases in case of strong $G$. We see in Fig. 6, the rise of $S_i$ leads to an increase in velocity. A decreasing affect on velocity field for $P_i$ is observed from Fig. 7.

The effect of the spin gradient viscosity number on the angular velocity field is displayed in Fig. 8 and we see that the angular velocity decreases with the rise of $\Lambda$. Fig. 9 shows, the angular velocity is increasingly affected by $\lambda$. The effect of Schmidt number on the angular velocity field is presented in Fig. 10 and an increasing effect on the angular velocity profiles are observed from the figure in case of strong $S_i$.

Fig. 11 represents the effect of $S_i$ on the induced magnetic field and it is observed from the figure the induced magnetic field decreases with the increase of $S_i$. A decreasing affect on induced magnetic field for $P_i$ is observed from Fig. 12. In Fig. 13, we see that the induced magnetic field increases in case of strong Prandtl number. An increasing effect on the fluid temperature for the Schmidt number is highlighted in Fig. 14.

The temperature distributions are shown in Figs. 15-16 for different values of $S_i$ and $P_i$. It is observed from the Fig. 15, the temperature weakly increases for the rise of $S_i$. The Fig. 16 shows that the temperature decreases with the rise of $P_i$.

For the different values of $P_i$ and $S_i$, the species concentration curves are displayed in Figs. 17-18. We see in Fig. 17, the species concentration decreases with the rise of $P_i$. A decreasing effect on the concentration profiles is observed from the Fig. 18.
Fig. 3. Velocity Profiles for $G_n = 1$, $G_r = 2$, $\Lambda = 1$, $\lambda = 1$, $S_r = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 4. Velocity Profiles for $G_n = 1$, $G_r = 2$, $\Lambda = 1$, $\lambda = 1$, $S_r = 1$, $M = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 5. Velocity Profiles for $G_n = 1$, $M = 1$, $\Lambda = 1$, $\lambda = 1$, $S_r = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 6. Velocity Profiles for $G_n = 1$, $G_r = 2$, $\Lambda = 1$, $\lambda = 1$, $M = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 7. Velocity Profiles for $G_n = 1$, $G_r = 2$, $\Lambda = 1$, $\lambda = 1$, $M = 1$, $D_r = 1$, $S_r = 1$, $P_r = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 8. Angular Velocity for $G_n = 1$, $G_r = 2$, $M = 1$, $\lambda = 1$, $S_r = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 9. Angular Velocity for $G_n = 1$, $G_r = 2$, $M = 1$, $\Lambda = 1$, $S_r = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_r = .01$.

Fig. 10. Angular Velocity for $G_n = 1$, $G_r = 2$, $M = 1$, $\lambda = 1$, $S_r = 1$, $D_r = 1$, $P_r = .71$, $P_m = 1$, $\Delta = 1$, $\alpha = 1$, $\Lambda = 1$, & $E_r = .01$. 

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Fig. 11. Induced Magnetic Field for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $M = 1$, $D_a = 1$, $P_a = .71$, $P_b = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 12. Induced Magnetic Field for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $M = 1$, $D_a = 1$, $P_a = .71$, $S_c = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 13. Induced Magnetic Field for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $M = 1$, $D_a = 1$, $S_c = 1$, $P_a = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 14. Induced Magnetic Field for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $M = 1$, $D_a = 1$, $P_a = .71$, $P_b = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = 1$, & $E_c = .01$.

Fig. 15. Temperature for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $\lambda = 1$, $M = 1$, $D_a = 1$, $P_a = .71$, $P_b = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 16. Temperature for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $\lambda = 1$, $M = 1$, $D_a = 1$, $S_c = 1$, $P_b = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 17. Concentration for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $\lambda = 1$, $M = 1$, $D_a = 1$, $S_c = 1$, $P_a = 1$, $\Delta = 1$, $\alpha = 1$, $S_c = .6$ & $E_c = .01$.

Fig. 18. Concentration for $G_a = 1$, $G_c = 2$, $\lambda = 1$, $\lambda = 1$, $M = 1$, $D_a = 1$, $S_c = 1$, $P_a = 1$, $\Delta = 1$, $\alpha = 1$, $P_a = .71$ & $E_c = .01$. 
Finally, a qualitative comparison of the recent result at steady-state with the previous result of the MHD free convection heat generating unsteady micropolar fluid flow through a porous medium given by Haque et al.[7] is presented in Table 1. In case of cooling of the plate, the present problem with the absence of the induced magnetic field reduces to the problem that investigated by Haque et al.[7]. The accuracy of the recent results may be described as good in case of all the flow variables.

Table 1: Qualitative comparison of the present result with previous result of approximate solutions

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<th>Increased Parameter</th>
<th>Previous Results due to Haque et al.[7]</th>
<th>Present Results of Numerical Solution</th>
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</table>

5. CONCLUSIONS

In this work thermal diffusion effects on the free convection heat and mass transfer MHD unsteady flow of a micropolar fluid through a porous medium with induced magnetic field is investigated. The resulting governing equations are solved by implicit finite difference method. The obtained results are graphically presented for the variations of associated parameters. Some of the important findings of this observation are given below:

i. For the cooling plate, the micropolar fluid velocity increases with the increase of Grashof number.

ii. The micropolar fluid velocity is more for air than water.

iii. The angular velocity is greater for heavier particle than lighter particle.

iv. The induced magnetic field is more for water than air.

v. The fluid temperature is higher for air than water.

vi. The species concentration is greater for heavier particle than lighter particle.

It is hoped that the findings of the present work may be useful for the study of astrophysics and geophysics.

6. REFERENCES


7. NOMENCLATURE

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<td>ϱ</td>
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8. MAILING ADDRESS

Md. Mohidul Haque  
Mathematics Discipline,  
Khulna University,  
Khulna-9208, Bangladesh  
E-mail: alam_mahmud2000@yahoo.com